

Towards Secondary Fingerprint Classification

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Abstract— This manuscript proposes a move towards the secondary level of fingerprint classification. This is done in order to further penetrate a fingerprint template database, and further reduce it to smaller partitions for efficient execution of the database search procedure. This is done through taking advantage of the extensibility of a structural fingerprint classifier when used on slapped, as opposed to rolled, fingerprints. The said classifier first orders a fingerprint into one of four primary fingerprint classes and, thereafter, into one of eight secondary fingerprint classes. Evaluated on the CSIR-Wits Fingerprint Database (CWFD), the primary classification module registers an accuracy figure of 80.4%, and the secondary classification module registers an accuracy figure of 76.8%. This small difference between the two figures is indicative of the validity of the proposed secondary classification module.

Keywords—fingerprint core; fingerprint delta; primary classification; secondary classification

I. INTRODUCTION

The classification of samples in an automated recognition system is primarily important because of the need to virtually divide the template database into smaller, manageable partitions. This virtual division is done before executing a database search procedure, and it is done in order to avoid having to search the entire template database and, for this reason, minimize the database search time and improve the overall performance of an automated recognition system. Sample classification is, at a secondary level, important because of its impact on the template database design process. This is because of the fact that, even a good database management system (DBMS) will be negatively affected by a poorly designed database [1]. Even though the concept of sample classification applies to systems that use almost any biometric modality, this manuscript focuses on fingerprint classification, with immediate application to an automated fingerprint recognition system. The commonly considered primary fingerprint classes are [2]: Central Twins (CT), Left Loop (LL), Right Loop (RL), Tented Arch (TA), and Plain Arch (PA). Many fingerprint classification practitioners, however, often reduce these five fingerprint classes to four. This is, at a high level, due to the difficulty in differentiating between the TA and the PA class. These two similar classes are often combined into what is referred to as the Arch (A) class. Recent examples of practitioners that have reduced the five-class problem to a four-class problem include Senior [3], Jain and Minut [4], and Yao *et al* [5].

These four primary classes are normally sufficient in the performance improvement of small-scale applications such as

access control systems and attendance registers of small to medium-sized institutions. They, however, may not be sufficient in the performance improvement of large-scale applications such as national Automatic Fingerprint Identification Systems (AFIS). In order to enforce visible performance improvement on such large-scale applications, this manuscript introduces a two-stage classification system, by exploiting the extensibility of the classification rules that utilize the locations of the fingerprint global landmarks, known as the singular points [6], on the fingerprint image foreground.

The first classification stage produces the primary fingerprint classes and then the second classification stage breaks each primary class into a number of secondary classes. It is important to note that the concept of secondary fingerprint classification, for structural fingerprint classifier, is one that has not been exploited by fingerprint classification practitioners. A structural fingerprint classifier is one that uses the arrangement of singular points in order to classify a fingerprint. The next section presents a detailed discussion of both the primary and the secondary fingerprint classes.

II. PRIMARY AND SECONDARY FINGERPRINT CLASSES

This section presents the proposed primary and secondary fingerprint classes, together with the rules used to determine them. As mentioned before, the rules used to determine these primary and the secondary classes are based on the arrangement of the fingerprint singular points, namely, the fingerprint core and the fingerprint delta. Forensically, a fingerprint core is defined as the innermost turning point where the fingerprint ridges form a loop, while the fingerprint delta is defined as the point where these ridges form a triangulating shape [7]. Figure 1 depicts a fingerprint with the core and delta denoted by the circle and the triangle, respectively.

A. Central Twins (CT) Primary Class and its Secondary Classes

Fingerprints that belong to the CT class are, at a primary level, those that have ridges that either form (i) a circular pattern, or (ii) two loops, in the central area of the print. Some practitioners usually refer to the circular pattern as a whorl [8], while the two-loop pattern is referred to as a twin loop [9]. The similarity, however, between the two patterns is that they both have cores located next to each other in the central area of the fingerprint, which is the main reason why Msiza *et al* [2] grouped these two patterns into the same class, called

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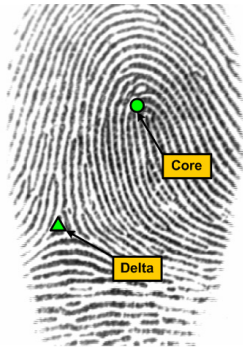


Figure 1. A fingerprint showing clear markings of the core (circle) and the delta (triangle)

the Central Twins class. Figure 2(a) shows the whorl pattern, while the twin loop pattern is depicted on figure 2(b).

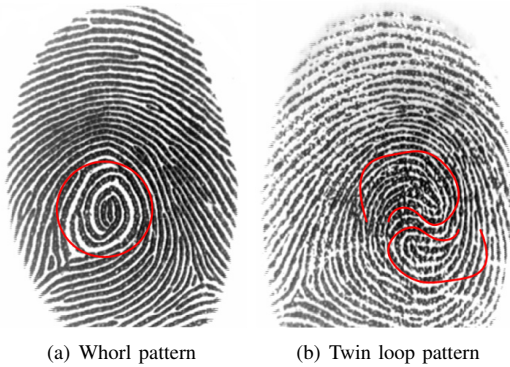


Figure 2. Fingerprint patterns that collectively belong to the CT primary class. The whorl pattern has a circular structure that forms two cores, and the twin loop pattern has two loops that form two cores

In addition to the two cores located in the central area, fingerprints belonging to CT class also have two deltas. These two deltas, however, are not located in the central area of the print, which immediately implies that there is a chance that one, or even both, may not be captured. All of this is dependent on how the user or subject impresses their finger, for capturing, on the surface of the fingerprint acquisition device. This is what brings into point the possibility of deriving secondary classes of this CT primary class.

The CT secondary classes derived in this chapter are depicted in figure 3, and they add up to a total of three. Figure 3(a) shows a CT class fingerprint that has all the singular points captured, two cores and two deltas, which is an ideal case. Such a complete capture of information normally occurs in applications where fingerprints are rolled, instead of being slapped. This is because of the fact that deltas, in fingerprints that belong to the CT primary class, are normally located adjacent to the edges of the fingerprint ridge area. A CT class fingerprint that has two cores and two deltas captured, is assigned to what is introduced as the CT-1 secondary class. A CT class fingerprint that has two cores and one delta, as shown in figure 3(b), is assigned to what is introduced as the CT-2

secondary class while the one that has two cores and no delta, as depicted in figure 3(c), is assigned to what is introduced as the CT-3 secondary class.

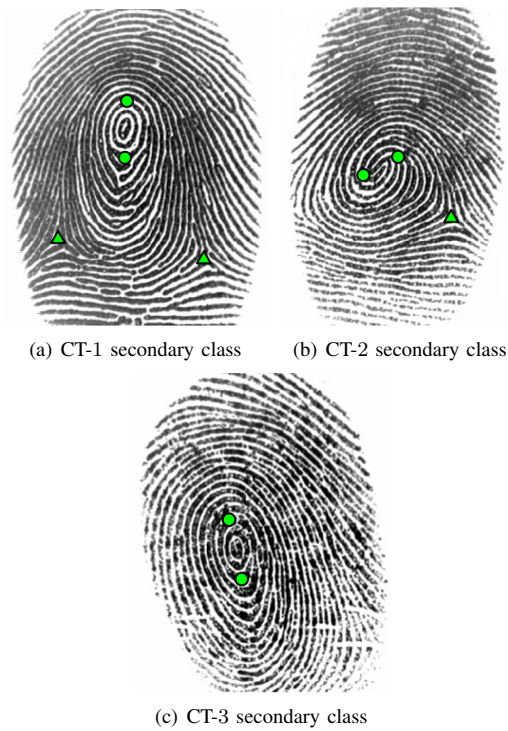


Figure 3. Fingerprint patterns that determine the CT secondary classes. CT-1 class: 2 cores & 2 deltas; CT-2 class: 2 cores & 1 delta; and CT-3 class: 2 cores & no delta

B. Arch (A) Primary Class and its Secondary Classes

Fingerprints that belong to the A class are, at a primary level, those that have ridges that appear to be entering the fingerprint on one side, rise in the middle area of the fingerprint, and leave the fingerprint on the opposite side, as depicted in figure 4. Figure 4(a) shows a fingerprint pattern that some practitioners normally classify as a plain arch, while figure 4(b) depicts a pattern that some practitioners classify as a tented arch. The technical report of Hong and Jain [10] is one example of the practice of ordering these two patterns into separate classes. A year later, however, Jain *et al* [11] realized that there is often a mis-classification between the two patterns, hence it is better to combine them into one class. Many other practitioners, including Msiza *et al* [2], have observed that combining the plain arch and the tented arch patterns into one class, does improve the classification accuracy.

Because of this reality, it is proposed that these two patterns are better off at a secondary level of fingerprint classification. This immediately provides a platform for the proposition of a number of A class secondary rules. An A class fingerprint that is without both a core and a delta, is assigned to what is introduced as the A-1 secondary class. Msiza *et al* [2] suggest that, for an A class fingerprint that has a core and delta detected, the absolute difference between their x -coordinates, Δx , is less

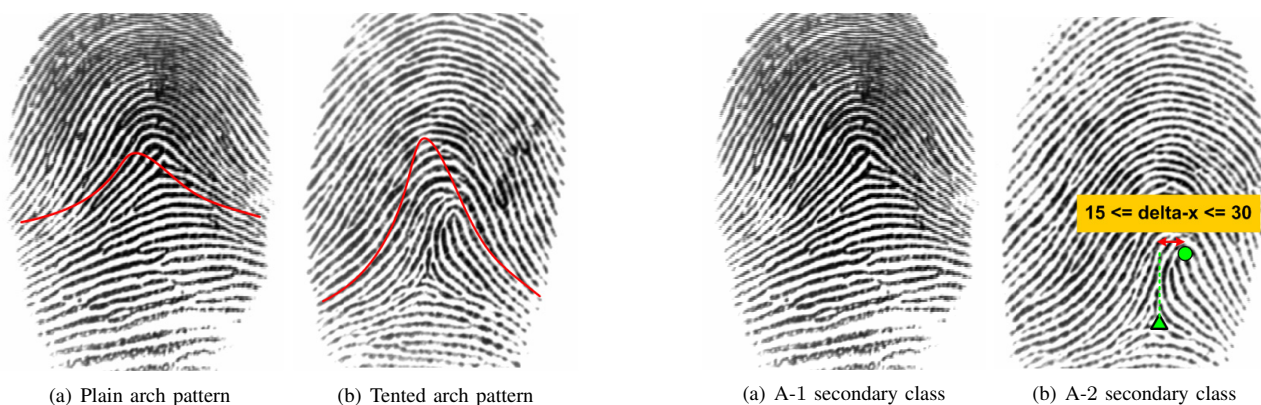


Figure 4. Fingerprint patterns that collectively belong to the A primary class. The plain arch pattern has no singular points while the tented arch pattern has a core and a delta, with the delta located almost directly below the core

than or equal to 30 pixels. It is, for this reason, proposed that if an A class fingerprint has a core and delta detected; and Δx is between 30 and 15 pixels, then the fingerprint is assigned to what is introduced as the A-2 secondary class; else if Δx is between 15 and 0 pixels, then fingerprint is assigned to what is introduced as the A-3 secondary class. The instances where Δx is between 15 and 0 pixels happens when the rise of the ridges in the middle part of the fingerprint is extremely acute, hence Δx is extremely small. Figure 5 depicts all three A secondary fingerprint classes.

C. Left Loop (LL) Primary Class and its Secondary Classes

Fingerprints that belong to the LL class are, at a primary level, those that have ridges that appear to be entering the fingerprint on the left hand side, make a loop in the middle area of the fingerprint, and leave the fingerprint on the same side where they entered. The loop in the middle area is what forms the core of the print. An example of a fingerprint that belongs to this class is depicted on figure 6. In addition to the core that is formed by the loop in the middle area, an LL fingerprint has a delta located at the bottom of the loop, adjacent to the right hand side edge of the print. Depending on how the finger is impressed against the surface of the capturing device, there is always a chance that the delta may not be captured, more especially because it is adjacent to the edge of the fingerprint. This, therefore, presents an opportunity for the formulation of two LL secondary classes.

If a fingerprint that belongs to the LL class has (i) both a core and a delta detected, (ii) the conjugate slope (C-Slope) of the line joining the core and the delta is negative, and (iii) $\Delta x > 30$ pixels, then this fingerprint is assigned to what is introduced as the LL-1 secondary fingerprint class. The said C-Slope is just a complement of the conventional slope, because its reference point, or origin, is not the geometric center of the fingerprint image, but is the top left hand corner of the image. The LL-1 classification rules are summarized in figure 7(a).

If a fingerprint that belongs to the LL class has only a core detected and – when a Cartesian plane, whose origin is the True Fingerprint Center Point (TFCP), is drawn on the

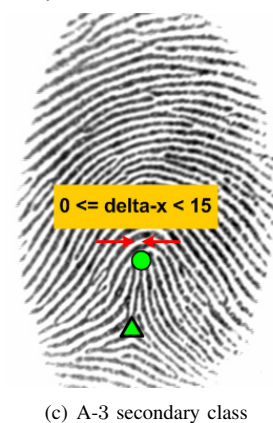


Figure 5. Fingerprint patterns that determine the A secondary classes. A-1 class: 0 cores & 0 deltas; A-2 class: Δx between 30 pixels and 15 pixels; and A-3 class: Δx between 15 pixels and 0 pixels



Figure 6. A fingerprint pattern that belongs to the LL primary class. The ridges enter the print on the left hand side, make a loop in the middle, and leave on the same side

fingerprint ridge area – the core is located either in the first or the fourth quadrant, then the fingerprint is assigned to what is introduced as the LL-2 secondary class. The TFPC is defined as the geometric center of the fingerprint ridge area, that is, the fingerprint foreground [12]. Figure 7(b) shows a fingerprint that belongs to the LL-2 secondary class, with its core located in the first quadrant.

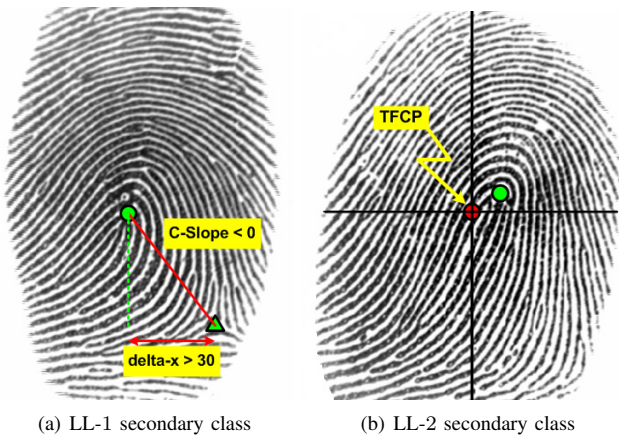


Figure 7. Fingerprint patterns that determine the LL secondary classes. LL-1 secondary class: 1 core & 1 delta, with C-Slope < 0; and LL-2 secondary class: 1 core & 0 delta, with the core located in the first quadrant

D. Right Loop (RL) Primary Class and its Secondary Classes

Fingerprints that belong to the RL class are, at a primary level, those that have ridges that appear to be entering the fingerprint on the right hand side, make a loop (which forms a core) in the middle area of the fingerprint, and leave the fingerprint on the same side where they entered. An example of a fingerprint that belongs to this RL class is depicted on figure 8. In addition to the core that is formed by the loop in the middle, an RL fingerprint has a delta located at the bottom of the loop, adjacent to the left hand side edge of the print. Similarly, depending on how the finger is impressed against the capturing device, there is always a chance that the delta may not be captured, more especially because it is adjacent to the edge of the fingerprint. This, therefore, presents an opportunity for the formulation of two RL secondary classes.



Figure 8. A fingerprint pattern that belongs to the RL primary class. The ridges enter the print on the right hand side, make a loop in the middle, and leave on the same side

If a fingerprint that belongs to the RL class has (i) both a core and a delta detected, (ii) the C-Slope of the line joining the core and the delta is positive, and (iii) $\Delta x > 30$ pixels, then this fingerprint is assigned to what is introduced as the RL-1 secondary fingerprint class. If a fingerprint that belongs to the RL class has only a core detected and the core is located

either in the second or the third quadrant, then the fingerprint is assigned to what is introduced as the RL-2 secondary class. These two secondary classification rules are summarized in figure 9.

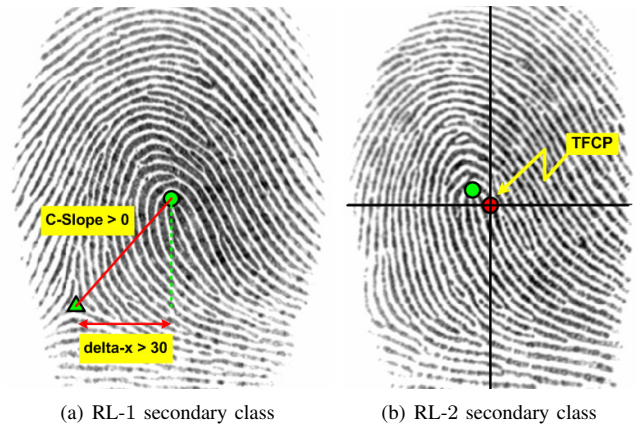


Figure 9. Fingerprint patterns that determine the RL secondary classes. RL-1 secondary class: 1 core & 1 delta, with C-Slope > 0; and LL-2 secondary class: 1 core & 0 delta, with the core located in the second quadrant

E. Classes Overview

Following the proposed primary and secondary classes, figure 10 presents a combined picture that shows the relationship between all of them. The primary classification layer consists of 4 instances, while the secondary classification layer consists of a total of 10 instances.

III. IMPLEMENTATION OF THE PROPOSED CLASSIFICATION SCHEME

The implementability of the proposed classification scheme is demonstrated through the pseudo-code presented in algorithm 1. It is important to note that, before classification can be done, the captured fingerprint has to go through some pre-processing. These pre-processes include contrast enhancement [13], ridge segmentation [14], orientation image computation and smoothing [15], and singular point detection [6]. The credibility of this proposed classification scheme is evaluated, in two different ways, in the next section.

IV. CLASSIFIER PERFORMANCE EVALUATION

In order to evaluate the credibility of the idea of secondary fingerprint classification, it is important to measure the accuracy of both the primary and the secondary classification module. If this idea is indeed credible, the difference between the accuracy value of the primary module and the one of the secondary module should be small. It should be small to an extent that it should tempt any fingerprint classification practitioner to, in future applications, consider using the proposed secondary fingerprint classes as primary classes.

In addition to the accuracy values, the proposed classification scheme's credibility should be evaluated through observing the time it takes a fingerprint recognition system to search through a template database (i) without any classification, (ii)

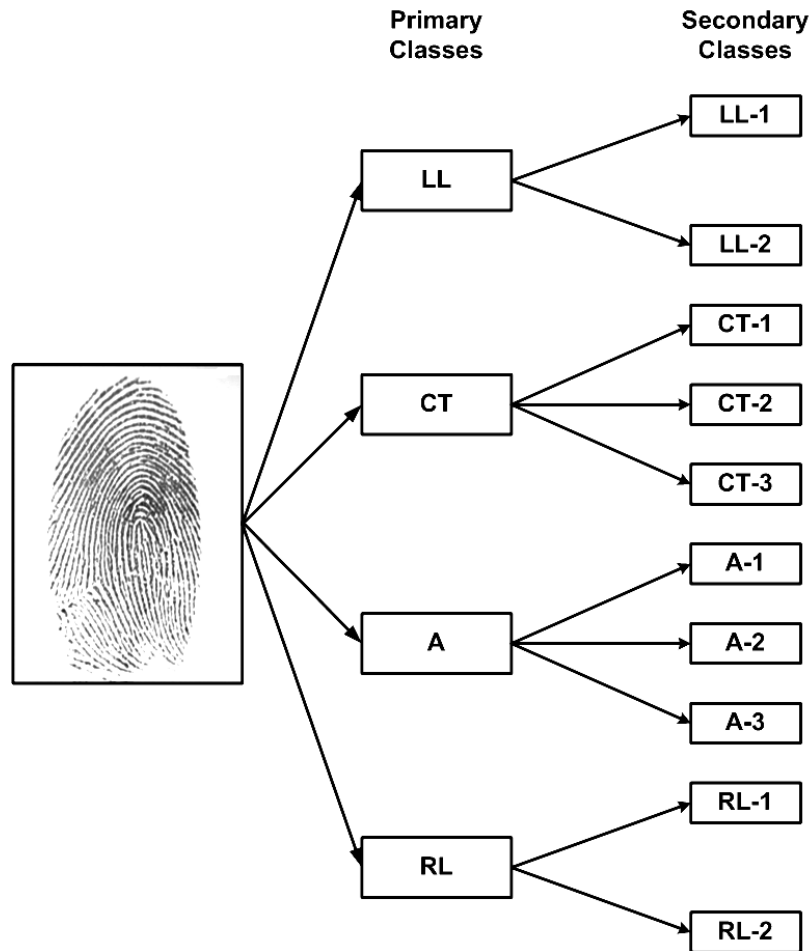


Figure 10. An overview of the proposed primary and secondary fingerprint classes

with only the primary classification module, and (ii) with the secondary classification module. For this classification scheme to be regarded as credible, the average database search time for cases (ii) and (iii) must be less than that for case (i), and the one for case (iii) should be less than the one for case (ii), while the matching rates remain significantly unchanged. For the purposes of this evaluation, the CSIR-Wits Fingerprint Database (CWFD) which was jointly collected, for academic research purposes, by the Council for Scientific & Industrial Research (CSIR) and the University of the Witwatersrand (Wits), both in the Republic of South Africa.

A. Classification Rates

This section presents the classification accuracy values, in the form of confusion matrices, of both the primary and the secondary classification modules. A confusion matrix is a table that shows a summary of the classes assigned by the automated fingerprint classifier, measured against those assigned by a human fingerprint classification expert. The classification accuracy value is mathematically expressed as:

$$Accuracy = \frac{M}{T} \times 100\%, \quad (1)$$

where M is the sum of the main diagonal of the matrix, and T is the sum of all the instances of data in the chosen database. Evaluated on a database that contains 946 instances, table I shows the confusion matrix for the primary classification module, while table II shows the confusion matrix of the secondary classification module.

Table I displays a classification accuracy of 80.4%, which is an acceptable figure for a four-class problem. As an example, Senior [16] obtained a classification accuracy of 81.6% for his four-class problem. Some of the A class fingerprints are misclassified as LL and RL because it is not all of them that have a Δx that is less than 30 pixels. Possible future improvements, therefore, involve a bit more experimentation on a range of Δx values. Some of the CT class fingerprints are misclassified as A possibly because the singular point detection module was unable to detect the cores of the fingerprints. A possible future improvement, therefore, involves working on the functionality of the singular point detection module. Some of the LL class fingerprints are misclassified as A because it is not all the LL fingerprints that have a Δx that is greater than 30 pixels, and the same reasoning can be attributed to the mis-classification of some of the RL class fingerprints. Possible

Algorithm 1: The main procedure that, when presented with singular points, determines both a fingerprint's primary and secondary class

Input : Fingerprint singular points

Output: Fingerprint primary and secondary class

```

begin
  initialize: primary class = unknown, and secondary
  class = unknown;
  calculate: the number of cores,  $N_C$ , and the number
  of deltas,  $N_D$ , detected;
  if  $N_C = 0$  and  $N_D = 0$  then
    | use algorithm 2 for classification;
  end
  else if  $N_C = 1$  and  $N_D = 0$  then
    | use algorithm 3 for classification;
  end
  else if  $N_C = 1$  and  $N_D = 1$  then
    | use algorithm 4 for classification;
  end
  else if  $N_C = 2$  and  $N_D$  is between 0 and 2 then
    | use algorithm 5 for classification;
  end
end

```

Algorithm 2: A procedure that, when presented with neither core nor delta, determines both a fingerprint's primary and secondary class

Input : Zero core and zero delta

Output: Fingerprint primary and secondary class

```

begin
  | primary class = A;
  | secondary class = A-1;
end

```

future improvements, again, involve a bit more experimentation on a range of Δx values.

The secondary classification accuracy in table II has a value of 76.8%, which is an encouraging figure for a newly introduced concept. This implies that there is a difference of only 3.6% between the primary and the secondary classification modules. This, therefore, provides future opportunities for a classification practitioner to fine-tune the secondary classification rules in order to further close down the gap between the two classification modules. As soon as this gap approaches zero, these newly introduced secondary classes can be used as primary classes and, with a total of 10 primary classes, there will be countless opportunities to further reduce the database search time. This is achievable through the introduction of another set of secondary classes by using unsupervised techniques such as artificial neural networks [17].

Algorithm 3: A procedure that, when presented with one core and no delta, determines both a fingerprint's primary and secondary class

Input : One core and zero delta

Output: Fingerprint primary and secondary class

```

begin
  compute: the True Fingerprint Center Point (TFCP);
  if the core is located in the 1st or 4th quadrant then
    | primary class = LL;
    | secondary class = LL-2;
  end
  else if the core is located in the 2nd or 3rd quadrant
  then
    | primary class = RL;
    | secondary class = RL-2;
  end
end

```

Algorithm 4: A procedure that, when presented with one core and one delta, determines both a fingerprint's primary and secondary class

Input : One core and one delta

Output: Fingerprint primary and secondary class

```

begin
  compute: the absolute difference,  $\Delta x$ , between the
   $x$ -coordinates;
  if  $\Delta x \leq 30$  pixels then
    | primary class = A;
    | if  $\Delta x \geq 15$  pixels then
      | secondary class = A-2;
    end
    | else if  $\Delta x < 15$  pixels then
      | secondary class = A-3;
    end
  end
  if  $\Delta x > 30$  pixels then
    compute: the C-Slope of the line joining the core
    and the delta;
    | if C-Slope is Positive then
      | primary class = RL;
      | secondary class = RL-1;
    end
    | else if C-Slope is Negative then
      | primary class = LL;
      | secondary class = LL-1;
    end
  end
end

```

B. Average Search Times and Matching Rates

To further demonstrate the credibility of the proposed classification scheme, this section presents its performance

TABLE II
 THE SECONDARY CLASS EXPERIMENTAL RESULTS TESTED ON THE CWFD, WHICH CONTAINS 946 DATA INSTANCES

Actual	As										Total
	A-1	A-2	A-3	CT-1	CT-2	CT-3	LL-1	LL-2	RL-1	RL-2	
A-1	118	01	01	00	00	03	03	05	00	23	154
A-2	05	17	02	00	00	00	02	01	00	05	33
A-3	06	02	48	00	00	00	05	09	00	08	77
CT-1	00	00	00	00	00	00	00	00	00	00	00
CT-2	03	00	00	00	16	03	00	00	00	00	22
CT-3	14	00	01	00	07	161	00	05	01	09	198
LL-1	00	00	00	00	00	00	09	00	00	02	11
LL-2	07	03	00	00	03	05	03	140	01	03	165
RL-1	02	00	00	00	00	00	00	00	09	00	11
RL-2	24	03	00	00	00	11	02	22	04	209	275
76.8%											946

Algorithm 5: A procedure that, when presented with two cores and zero or a few deltas, determines both a fingerprint's primary and secondary class

Input : Two cores and zero or a few deltas

Output: Fingerprint primary and secondary class

begin

primary class = CT;

calculate: the exact number of deltas, N_D , detected;

if $N_D = 0$ **then**

 | secondary class = CT-3;

end

else if $N_D = 1$ **then**

 | secondary class = CT-2;

end

else if $N_D = 2$ **then**

 | secondary class = CT-1;

end

end

a matching threshold T , the TMR value of T is the number of genuine comparisons with match scores greater than T , divided by the total number of genuine samples, S_G , presented for comparison. Mathematically, this is modeled as:

$$TMR = \frac{Count\{C_G \geq T\}}{S_G} \times 100\%. \quad (2)$$

A false match occurs when a fingerprint recognition system regards an impostor comparison, C_I , as genuine. The FMR value of T is the number of impostor comparisons with match scores greater than T , divided by the total number of impostor samples, S_I , presented for comparison. Mathematically, the FMR can be modeled as:

$$FMR = \frac{Count\{C_I \geq T\}}{S_I} \times 100\%. \quad (3)$$

A true non-match occurs when a fingerprint recognition system correctly regards an impostor comparison as an impostor. The TNMR value of T is the number of impostor comparisons with match scores less than T , divided by the total number of impostor samples presented for comparison. Mathematically, this can be modeled as:

$$TNMR = \frac{Count\{C_I < T\}}{S_I} \times 100\%. \quad (4)$$

A false non-match occurs when the fingerprint recognition system regards a genuine comparison as an impostor. The FNMR value of T is the number of genuine comparisons with match scores less than T , divided by the total number of genuine samples presented for comparison. Mathematically, this can be modeled as:

$$FNMR = \frac{Count\{C_G < T\}}{S_G} \times 100\%. \quad (5)$$

Table III shows the results obtained from the evaluation, where 3 instances of the same fingerprint were enrolled into the template database, in order to make the system more accurate. The template database, for this reason, ended up with a total of $3 \times 86 = 258$ instances. The credibility of the proposed classification scheme is verified by the fact that the average database search time (AST) is improved from 2 426 ms

 TABLE I
 THE PRIMARY CLASS EXPERIMENTAL RESULTS TESTED ON THE CWFD, WHICH CONTAINS 946 INSTANCES OF DATA

Actual	As				Total
	A	CT	LL	RL	
A	200	03	25	36	264
CT	18	187	05	10	220
LL	10	08	152	06	176
RL	29	11	24	222	286
80.4%					946

when measured through the average database search time, together with the matching rates, also done on the CWFD. These matching rates are the True Match Rate (TMR), the False Match Rate (FMR), the True Non-Match Rate (TNMR), and the False Non-Match Rate (FNMR).

A true match occurs when a fingerprint recognition system correctly regards a genuine comparison, C_G , as genuine. Given

to 645 ms and 492 ms by the primary and the secondary classification module, respectively, while the matching rates remain significantly unchanged.

TABLE III
A SUMMARY OF THE MATCH AND NON-MATCH RATES TOGETHER WITH THE AVERAGE DATABASE SEARCH TIMES, TESTED ON THE CWFD

	No Classification	Primary Classification	Secondary Classification
TMR	78.3%	70.4%	66.2%
FMR	0.7%	0.2%	0.1%
TNMR	99.3%	99.1%	99.2%
FNMR	21.6%	32.2%	30.2%
AST	2 426 ms	645 ms	492 ms

Because the TMR and the FNMR are complements of each other, their values should add up to a 100%. For the same reason, the values of the FMR and the TNMR should add up to a 100%. The reason why this is not case in the third and the fourth columns of table III is that the database search was done continuously per group of fingerprint instances of a common subject, which leads to a loss of data. This loss of data is, in essence, attributable to a combination of possible mis-classifications and failure to meet the matching threshold.

V. DISCUSSIONS AND CONCLUSIONS

This chapter presented the concept of automatic fingerprint classification, in general, and introduced the concept of secondary fingerprint classification, in particular. Secondary fingerprint classification was introduced in order to further reduce the time it takes for an automated fingerprint recognition system to search through a database of templates. The key fingerprint features employed in the proposed classification scheme are the core and the delta, with a total of 4 primary fingerprint classes; namely: CT, A, LL, and RL; and 10 secondary fingerprint classes, namely: CT-1, CT-2, CT-3, A-1, A-2, A-3, LL-1, LL-2, RL-1, and RL-2. Using a confusion matrix as a performance measure, the primary fingerprint classification module registered an accuracy of 80.4%, while the secondary classification module registered an accuracy of 76.8%. This 3.6% gap is indicative of the fact that, in future applications, there is a chance to fine-tune the secondary classification rules and, after improving the accuracy, there is even a good chance to use these secondary classes at a primary level. With a total of 10 fingerprint classes at a primary level, there is a good chance of decreasing the database search time even further, while the change in matching rates remains acceptably small.

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